Game Starts at GameStop: Characterizing the Collective Behaviors and Social Dynamics in the Short Squeeze Episode

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Abstract—In January 2021, the users of subreddit r/wallstreetbets (WSB) triggered an unprecedented short squeeze by driving up GameStop’s stock price to an unimaginable high point. During the event, a large number of users participated in the discussion about GameStop and coordinated trading behavior on r/WSB to push the stock price higher. In this article, we investigate the characteristics of the collective behaviors and social dynamics from the evolutions of topological structure, discussed topics, and user sentiment polarity (SP) by constructing dynamic interaction networks, modeling the topic, and analyzing the user sentiment. We find that the topological structure of the interaction network evolves toward a more efficient direction, the discussed topics change more centralized, and the user sentiment tends to be more positive and divergent. And we reveal that part of GameStop’s stock price is explained by the social media activity, popularity of the dominant topic, topic cohesiveness, SP of users, and sentiment divergence between interacted users on r/WSB. Our work quantitatively characterizes the interaction networks and user behavior during the GameStop short squeeze and provides an example to analyze the event which synchronously evolves in the physical space and cyberspace. It not only contributes to the analysis of social system behavior but also provides valuable insights into the financial practice and policy decision-making.

Index Terms— Dynamic interaction network, financial market, GameStop, short squeeze, social network analysis.

I. INTRODUCTION

IN JANUARY 2021, the biggest short squeeze of the decade took place on the New York Stock Exchange, causing major financial consequences for certain hedge funds and large losses for short sellers [1]. Due to the competition from digital distribution services, as well as the lockdown restrictions during the 2020 coronavirus pandemic, the public float of the American video game retailer GameStop (GME) was sold short by over 140% [2]. The users of the subreddit r/wallstreetbets (WSB), an Internet forum on the social news website Reddit, initially discussed their intentions to revolt against the short sellers and successfully triggered this short squeeze against the hedge funds by combining the buying power of retail investors to push GameStop’s stock price to an unimaginable point. As of January 27, 2021, the short squeeze resulted in a 1700% increase in GameStop’s close price, reaching U.S. $347.51 from U.S. $17.25 at the ending of the last month [3]. At the end of January, the unusually high price made Melvin Capital that heavily shorted GameStop lose 53% of its investments [4].

The GameStop short squeeze is the first time the retail investors coordinated with each other via social media platforms and fulfilled their plan of squeezing short to change the trading landscape [5]–[7]. It reveals the potential power that a growing force of retail investors can wield in stock markets when equipped with social media. The traditional financial transaction mode has changed with the rapid development of the Internet and social networks [8], [9]. The game of retail investors banding together to impact the financial market has just started. We must pay great attention to this emerging social phenomenon and deeply investigate its internally collective behavior and social dynamics mechanism.

The GameStop short squeeze highlights the significant role of social media in the propagation of investment ideas and the coordination of collective behaviors [10], [11] and produces many research questions about analyzing the behavioral characteristics of participants on social media during the GameStop frenzy [12]. In fact, during the event, a large number of users participated in the discussion about GameStop and coordinated their trading behaviors on r/WSB to push the surge of stock price while forming dynamic interaction networks. Characterizing the social networks under the GameStop short squeeze background with the quantitative technologies not only contributes to the analysis of social system behavior but also provides valuable insights into the financial practice and policy decision-making.

Several preprints exist to analyze the GameStop short squeeze from various viewpoints [13]–[17]. The generating
mechanism of a short squeeze and its impediment to market quality were the first to be explored [13], [14] from the perspective of financial theory. Vasilieou [15] next confirmed that the GameStop short squeeze leads to market abnormality and antileverage effect, which provides a new way to econometrically show a violation of the efficient market hypothesis (EMH). Angel [16] proposed that the short squeeze reveals several loopholes in the system of the U.S. equity market that need to be plugged. From the viewpoint of social media, Lyócsa et al. [38] utilized the level of activity on r/WSB and the search volume of Google to explain the variation of the stock price. Angel [16] presented a dynamics model that unifies naive investors, fanatical investors, rational short-term investors, and long-term investors in a social network to study the observed phenomena in the events of GameStop. Long et al. [17] found that the comment sentiments extracted from r/WSB influence GameStop’s intraday returns.

In summary, the existing works offer noticeable insights on the GameStop short squeeze from both financial and social media perspectives. However, it is empirically unknown to the researchers how the stock market is interconnected with social media activity (SMA) and the potential characteristics of collective behaviors and social dynamics during the short squeeze frenzy. There are few large-scale empirical investigations on participants’ behaviors in the social networks, which forms an unprecedented force to push the stock prices soaring. Fortunately, the subreddit r/WSB containing mass social history records is a natural experimental site to explore the behavioral characteristics of users in the formed dynamic interaction networks.

In this article, by constructing and analyzing the dynamic interaction networks between users, we investigate the critical characteristics of user behavior on r/WSB during the short squeeze and how they are likely to influence the information spreading and the volatility of the financial market. We first explore the evolutional dynamics characteristics of topological structure of dynamic interaction networks by analyzing several network statistics. Then, we obtain the basic perceptions for the user behavior in the dynamic interaction networks by executing quantitative analysis from two aspects: 1) the topic modeling and 2) sentiment analysis. In particular, for the discussed topics on r/WSB, we propose a user topic embedding method to investigate the topic evolution from the individual level to the community level and compare the difference between influential users and common users. For the investment sentiment, we explore the evolutional characteristics of the sentiment polarity (SP) and measure the sentiment homophily and divergence. Lastly, to study the relationship between the market and social media, we explain GameStop’s price trend by modeling the relationship between price response and five explanatory variables derived from the topic and sentiment characteristics.

The main contributions of this article are twofold.
1) We quantitatively depicted the evolutional characteristics of interaction networks and user behavior during the GameStop short squeeze and provide a case study to analyze the event which synchronously evolves in the physical space and cyberspace. The findings in this article may provide insight to regulate financial behaviors.
2) We constructed five factors from the evolutions of dynamic networks and topic and sentiment characteristics to explain the association between GameStop’s price trend and the social behavior of retail investors. It also provides a new and parsimonious way to analyze and predict the stock price from the unstructured social media data.

II. DATA

In this section, we first split the short squeeze event into five phases according to some remarkable events that significantly promote the GME short squeeze development. Then, we present a brief description of the WSB dataset. Next, we report the construction of dynamic user interaction networks. Last, we introduce the sentimental polarity dictionary used in this work.

A. Timeline

To explore the interaction between social media and the financial market, we acquired the stock price data of GameStop from Barchart. To untangle the development of the short squeeze, we divide the event into five phases: prehistory, incubation, development, climax, and fade, according to some important signs that significantly promote the evolution of the GME short squeeze. The detailed information is shown in Table I. We carefully reviewed the process of the short squeeze event and thought that GameStop Corp’s announcement that Ryan Cohen and his two partners will be the directors on GameStop’s board is the prolog of the event because GameStop’s stock price continually rises and finally surges after the announcement. During its development, the battle between Angel and the retailers of r/WSB accelerating the rise of GameStop’s price can be seen as a demarcation point from incubation to development. That Elon Musk tweeted “GameStonk!!” sharply pushed up the stock price and made the short squeeze into climax. After February 1, 2021, the continual decline of stock price means that the price frenzy fades. The overall development process can be seen in Fig. 1.

B. WSB Dataset

To perform an empirical analysis about the behavioral characteristics of participants, we collected more than 9 million unique pieces of content, including posts and comments from 8, 2020 to February 3, 2021 from r/WSB using the Pushshift API.4 Hereafter, we call the collection WSB dataset.

1https://www.reuters.com/article/us-gamestop-ryan-cohen-idUSKBN29GIEF
2https://twitter.com/CitronResearch
3https://twitter.com/elomusk
4https://www.cnbc.com/2021/02/01/gamestop-shares-reddit-trader-frenzy-continues-into-february.html
5https://www.barchart.com/
6Pushshift API is an important tool to obtain big data from various social media companies such as Twitter and Reddit. Its main page is https://pushshift.io/.
TABLE I

<table>
<thead>
<tr>
<th>Phase</th>
<th>Remarkable event</th>
<th>Date range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prehistory</td>
<td>No remarkable event.</td>
<td>12/08/20-01/11/21</td>
</tr>
<tr>
<td>Incubation</td>
<td>Announcement of board refreshment to accelerate transformation1.</td>
<td>01/12/21-01/18/21</td>
</tr>
<tr>
<td>Development</td>
<td>Comment from Citron Research predicting the value of the stock would decrease2.</td>
<td>01/19/21-01/25/21</td>
</tr>
<tr>
<td>Climax</td>
<td>Elon Musk tweeted “Gamestonk!!!”3.</td>
<td>01/26/21-01/31/21</td>
</tr>
<tr>
<td>Fade</td>
<td>Continual of decline of GameStop’s price4.</td>
<td>02/01/21-02/03/21</td>
</tr>
</tbody>
</table>

Fig. 1. Diagram of the development of the short squeeze.

TABLE II

<table>
<thead>
<tr>
<th>Phase</th>
<th>#Post</th>
<th>#Comment</th>
<th>#User</th>
<th>Date range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prehistory</td>
<td>34350</td>
<td>1885554</td>
<td>107698</td>
<td>12/08/20-01/11/21</td>
</tr>
<tr>
<td>Incubation</td>
<td>15724</td>
<td>653585</td>
<td>65146</td>
<td>01/12/21-01/18/21</td>
</tr>
<tr>
<td>Development</td>
<td>23829</td>
<td>819950</td>
<td>100071</td>
<td>01/19/21-01/25/21</td>
</tr>
<tr>
<td>Climax</td>
<td>335362</td>
<td>3124902</td>
<td>516775</td>
<td>01/26/21-01/31/21</td>
</tr>
<tr>
<td>Fade</td>
<td>372949</td>
<td>3333469</td>
<td>592021</td>
<td>02/01/21-02/03/21</td>
</tr>
</tbody>
</table>

The collected WSB dataset contains 6,330,271 posts and 8,666,673 comments which are submitted to the subreddit r/WSB from the period December 8, 2020 to February 3, 2021. Due to some technical reasons, the Pushshift sever did not ingest the intraday data from Reddit on January 25, 2021 and January 26, 2021; thus, our WSB dataset excludes these days for the sake of simplicity. The detailed statistical descriptions are reported in Table II and Fig. 2.

C. Dynamic Interaction Networks

Given a set of posts crawled on r/WSB for someday, we retrieved all their comments to extract the social interaction between users. To accurately match the trading period of New York Stock Exchange, we regarded the data from 4:00 to 4:00 P.M. in the next day as a complete day. A user will be added into the network when the user first submits content, i.e., a post or comment on r/WSB at time t. If a user commented on another one’s post or commented at time t, we think there exists an edge between them after t. In this way, we can construct a user interaction network for each day.

D. SP Dictionary

Investor’s sentiment has been considered as an important aspect to analyze the economic and financial phenomena [18]–[20]. To investigate the investment sentiment of users on r/WSB, it is necessary to use an appropriate social media-orientated SP dictionary rather than a general sentiment dictionary. In this article, we utilize the NTUSD-Fin market sentiment dictionary [21] to calculate the users’ sentiment polarities for the market and GameStop. NTUSD-Fin is a market sentiment dictionary based on more than 330K labeled posts crawled from financial social media and contains 8331 words, 112 hashtags, and 115 emojis. A positive word score in NTUSD-Fin represents a bullish market SP.

III. METHOD

A. LDA Topic Model

As a classical generative statistical model for discovering the hidden semantic structures in a text body, latent Dirichlet allocation (LDA) is heavily used in financial text mining to extract the meaningful topics in a collection of documents [22]. LDA postulates that documents are produced from a mixture of topics and those topics are words’ probability distribution. In this article, we consider all statements of a user before time t on a particular day as a document and carry out LDA topic modeling to obtain the user’s topic. The idea that organizing the weight of each topic word into a vector to represent the user’s statement comes from the vector space perspective [23]. We describe the topic weight vector \( v_i \) as a user’s topic embedding where each element represents the proportion of a particular topic in a document. Furthermore, a given topic refers to a weighted sum of a series of words that have related meaning and appear in the document more frequently. Thus, we can get the representation for a single topic i by extracting top-n words’ weights \( c_i = [w_{ji}]^n_{j=1} \). The LDA is implemented using the Python library Gensim which is developed for topic...
modeling, document indexing, and similarity retrieval with large corpora.\footnote{https://radimrehurek.com/gensim/}

B. SP Identification

Due to the high cost of manually labeling the SP for the large-scale social media data, it is reasonable to use a lexicon and rule-based SP identification method. In this work, we adopt Valence Aware Dictionary and sEntiment Reasoner (VADER)\footnote{https://radimrehurek.com/gensim/} as the SP classifier, which is specifically attuned to sentiments expressed in social media. The used sentiment lexicon is reported in Section II-D. VADER generates several sentiment scores. We choose the compound score that is the most useful metric for polarity identification as the final sentiment score. The compound score is computed by summing the valence scores of each word in the lexicon, adjusted according to the rules, and then normalized to be between $-1$ (most extreme negative) and $+1$ (most extreme positive).

IV. TOPOLOGICAL CHARACTERISTICS OF INTERACTION NETWORKS

In this section, we mainly concern the topological structure and statistical description of our constructed user interaction networks. We first present the changes of structural indicators of the network over time, including the number of nodes and edges, density, average degree, diameter, and average shortest-path length. Then, several nontrivial topological features are examined, including the assortativity, clustering, and centrality. We finally verify whether these interaction networks are scale free and small world.

To describe the dynamic response of social forum r/WSB to the GameStop squeeze, we build the user interaction network each day. We present the basic topological features, including the number of nodes and edges, density, average degree, diameter, and average shortest-path length in Fig. 3. From the shape perspective, the curves of the number of nodes and edges are similar to GameStop's close price curve. We can see that the number of nodes fluctuates smoothly in the prehistory and incubation phases, rises slightly in the development phase, leaps upward in the climax phase, and drops dramatically during the fade. A significant decrease in the density and the average degree during the GameStop short squeeze is entirely predictable because of the expansion of the network scale. On the contrary, the diameters of user interaction networks rise with the expansion of the network scale.

Another interesting phenomenon is that the networks' average shortest-path lengths do not scale to the massive sizes with the huge expansion of nodes. Instead, they slightly rise and decline in the development, climax, and fade phases compared with the dramatic changes of nodes and edges during the corresponding periods. It suggests that the user-generated interaction networks have low average shortest-path lengths. It has been proven that a network with a low average shortest-path length can provide efficient information diffusion\footnote{https://radimrehurek.com/gensim/}. Thus, the small average shortest-path length of the interaction network makes up the fundamental condition for the possibility that retailers efficiently communicate and coordinate on r/WSB to resist the shorting of institutional investors.

In addition to the direct structural description, we further calculated several nontrivial topological characteristics, including the degree assortativity, average clustering coefficient, average PageRank score, and average degree centrality. The degree assortativity measures the tendency for a network's nodes to attach to others that have similar degrees values\footnote{https://radimrehurek.com/gensim/}. Fig. 4(a) shows that the correlations between nodes of similar degree are negative and the values become more negative with the increase of the number of the nodes. In the context of the r/WSB, it means that more users tend to be connected with users with low degree values with the development of GameStop short squeeze. The reason behind is that more common users/low degree users build interactions with those influential users/high degree users by commenting on influen-
Fig. 5. Degree distribution of the interaction network on some example days. The chosen dates cover all five phases defined in Table I. (a) December 26, 2020. (b) January 15, 2021. (c) January 22, 2021. (d) January 28, 2021. (e) February 1, 2021. (f) Kolmogorov–Smirnov test for the power-law distribution. In this article, we set the significance level as 0.05.

The clustering coefficient represents the degree to which nodes in a network tend to cluster together [25]. The average of daily average clustering coefficient is 0.122, which is slightly smaller than those social media for finding and creating friends such as Twitter and Facebook but is bigger than Yelp, Orkut, and Flickr [27], [28]. Moreover, we find that the average clustering coefficient tends to rise with fluctuation with the evolution of the GameStop event. Considering the smaller average shortest-path length shown in Fig. 3(f) during the last three phases, it is reasonable to think that the interaction network evolves toward the small-world network. That is, with the development of the GameStop event, most users can be reached from every other user by a small number of hops in the user interaction networks on r/WSB. Such topological property is conducive to the transmission of short squeeze intention to revolt against the short sellers.

Furthermore, we verify whether the user interaction networks are scale-free networks. For the constructed interaction network, we implement the Kolmogorov–Smirnov test that compares the fit distribution with the real network data [29]. We select the median dates for each phase to show the degree distribution and fit distribution in Fig. 5. The $p$-value of the Kolmogorov–Smirnov test is reported in Fig. 5(f). The test results indicate that the degree distributions follow the power law at the 0.05 significance level on most days, while the power law is invalid on January 27, 2021 and January 28, 2021 during the climax phase. Despite the data missing due to the server ban on January 27, 2021, a potential reason is that a large number of discussions outbreak on r/WSB, thus producing many high degree users on January 28, which makes the statistical test fail. The emergence of the scale-free property means that there exit some hubs in the user interaction networks [30]. We selected the top-10 users who have the highest PageRank score on r/WSB during the GameStop event. As shown in Table III, six of them are moderators on r/WSB. The other four common users have a large number of Karma which reflects how much the users’ contributions mean to the community. The emergence of the scale-free property and the category of influential users demonstrate a simple but important finding that most common users prefer to connect to the posts whose authors have considerable influence or certain popularity on r/WSB.

Overall, the users’ collective behaviors tend to form the interaction networks on r/WSB, which have the topological structural superiority to transport and boost the diffusion of the investment information. From the evolution perspective, the topological structure can dynamically change to respond to the financial market during the different development phases of the GameStop short squeeze. The interaction network evolves to a small network for efficient information transmission while keeping robust scale-free property with the surge of the stock price.

Table III

<table>
<thead>
<tr>
<th>User</th>
<th>User category</th>
<th>Karma</th>
</tr>
</thead>
<tbody>
<tr>
<td>u/grebfar</td>
<td>Moderator</td>
<td>118920</td>
</tr>
<tr>
<td>u/OPINION_IS_UNPOPULAR</td>
<td>Moderator</td>
<td>1517473</td>
</tr>
<tr>
<td>u/DeepFuckingValue</td>
<td>-</td>
<td>3695026</td>
</tr>
<tr>
<td>u/MotorizedDoucheCanoe</td>
<td>-</td>
<td>201530</td>
</tr>
<tr>
<td>u/TradeBaconFutures</td>
<td>Moderator</td>
<td>NULL</td>
</tr>
<tr>
<td>u/wallstreetboyfriend</td>
<td>-</td>
<td>108698</td>
</tr>
<tr>
<td>u/SignedUpWhilePooping</td>
<td>Moderator</td>
<td>22981</td>
</tr>
<tr>
<td>u/GoBeaversOSU</td>
<td>Moderator</td>
<td>160522</td>
</tr>
<tr>
<td>u/theycallmervan</td>
<td>-</td>
<td>252396</td>
</tr>
<tr>
<td>u/theycallme1</td>
<td>Moderator</td>
<td>109675</td>
</tr>
</tbody>
</table>

V. TOPIC ANALYSIS OF INTERACTION NETWORKS

The evolution of the topic is a side of users’ collective behaviors. This section examines the topic characteristics of the user-generated contents on r/WSB during the GameStop short squeeze. The interaction network evolves to a small network for efficient information transmission while keeping robust scale-free property with the surge of the stock price.

https://www.theverge.com/2021/1/27/22253251/discord-bans-the-r-wall streets-server
A. Individual Topic Evolution Analysis

Except for the evolution of topological structure, we must know what the users really discuss, how their concerned topics evolve during the GameStop short squeeze, and whether their trending topics are correlated with GameStop’s stock price.

We exploited word count to extract the top-10 most frequent words in each evolutional phase. All extracted keywords are shown in Table IV. As we expected, the terms about financial investment such as “stock,” “money,” and “buy” appear in all phases since r/WSB is a social forum where participants discuss stock and options trading. Meanwhile, the term “gme,” the GameStop Corporation’s ticker symbol, does not appear in the prehistory phase, indicating that few users focus on the GameStop’s stock. With the price of GameStop rising slowly in the incubation phase, the term “gme” emerges and the terms “buy” and “call” are the first two verbs about investment operation, which means that GameStop is the trending topic about investing. Similar hot topics appear in the development phase. It is noteworthy that the term “bb,” the BlackBerry Ltd.’s ticker symbol, emerges in the development phase, which satisfies the fact that bb is a company in a similar position to GameStop and a short squeeze about BlackBerry also is triggered during the GameStop short squeeze. The term “amc” appeared in the Climax phase is another company in a similar position to “gme” and “bb.” The term “hold” first appears in the climax phase because the war between long buyers and short sellers went to a critical moment in which the price reached a high point and some retailers started to sell shares. In that time, users on r/WSB called retailers to hold GameStop’s share and push the price to the moon. Moreover, brokerage service Robinhood halted the buying of GameStop, which aroused much online discussion on r/WSB. Thus, the term “robinhood” appears in the climax phase. During the fade phase, GameStop’s price plummeted and, therefore, the terms “buy,” “short,” “hold,” and “sell” are the keywords.

To better investigate the evolutional characteristics of topics, we define an LDA-based topic embedding for every user according to the user’s all posts and comments under the given phase. As the introduction about LDA-based topic embedding from Section III, each element of the embedding represents a topic weight. Furthermore, we can introduce a dominant topic label for each user by choosing the index of the maximum value of $p_i$, i.e., $l_i = \arg\max_j p_{ij} = [b_{i1}, \ldots, b_{ij}, \ldots, b_{i10}]$. The dominant topic label stands for the most likely tendency to some topic. Using t-Distributed Stochastic Neighbor Embedding (t-SNE) [31], [32], an unsupervised, non-linear technique primarily used for data exploration and visualizing high-dimensional data, we reduce the topic embedding into 2-D space for every user in each phase. The results of dimension reduction are shown in Fig. 6. It is clear that the users with the same topic roughly form a cluster and topics 8, 9, and 10 take a smaller proportion than topics 1, 2, and 3 in all phases.

To more clearly show the change of each topic, we calculated the proportion of users who focus on the same topic in each phase. From Fig. 7, we can observe that the proportions of the first four and first five topics gradually increase from prehistory to climax and the proportions of the last four and last five are compressed. We further extracted the top-10 topic words and only contained the word whose weight is greater than or equal to 0.01 for each topic. The topic words are reported in Table V. By jointly analyzing Fig. 7 and Table V, we discover that the proportions of topic 4 and topic 5 rise significantly in the climax and fade phases, respectively.
TABLE V

<table>
<thead>
<tr>
<th>Topic</th>
<th>Topic words</th>
<th>Topic words</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Money, lol, robinhood, account, make</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>Gme, still, amc, hold, moon, go</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>Share, buy, call, week, today, day, 1, 100, 10, sell</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>Buy, hold, sell, gme, still, stop, don't, can't</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>Us, people, wsb, know, guy, one, need, please, thanks, help</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>9Tendies means gains earned from an investment. The term is usually used by amateur investors day trading on Robinhood.</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>Stay, wtf, green, short, price, market, squeeze, share, gme, short, fund, hedge, sell</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>Like, stock, it's, gamestop, right, really</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>Fuck, shit, wait, guy, ill, hope, love, lmao</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>BB, let's, power, pltr, amc</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 8. Heat map of the Pearson correlation coefficient of daily topics. Please note that the data on January 25 and 26 are missing. We used the linear insertion method to complete the values.

B. Community Topic Evolution Analysis

Individual topic evolution analysis obtains an overall view of the topics on r/WSB. However, more extensive discussion about some topics usually takes place at the community level. Individual-level average topic embedding amplifies the personal statement and introduces noise. Thus, we construct a community-level LDA-based topic embedding to describe the topic distribution on r/WSB. For a community $i$ at time $t$, the community-level topic $c_{it}$ is defined as the average of community users, i.e., $c_{it} = (1/nt_i) \sum v_{ij}$, where $nt_i$ is the number of users in community $i$ and $v_{ij}$ is the topic embedding of user $i$ at time $t$. Then, the final topic embedding can be defined as $\tilde{d}_i = (1/nt_i) \sum n_{ij} c_{ij}$. By weighting the community topic, the final topic distribution makes a tradeoff between individual topics and community topic.

In this article, we use the Louvain method [33] to detect the communities in each daily interaction network. We visualized the final topic embedding in Fig. 9. We can find that topic 1 and topic 3 continually have high proportions before January 22. Topics 2 and 3 are the dominant topics during the climax phase. And topics 1–4 are the main topics during the fade phase.

Though we can observe an overall daily topic distribution, we still need to obtain the degree of topic dispersion in the user interaction network because the more dispersed the discussed topics are, the less information the topic distribution contains. Thus, we propose an index based on the community level topic to measure the topic cohesiveness (TC). We define the TC as the Kullback–Leibler (KL) divergence from 10-topic uniform distribution to $\tilde{d}_i$. The higher TC represents that the estimated topic distribution $\tilde{d}_i$ is more valuable. The daily TC is exhibited in Fig. 10. The cohesiveness first has a significant increase at the start of the incubation phase then falls to the normal level. From the development phase, the TC starts to rise rapidly again. The TC reveals the evolution of information quantity of topic distribution with the development of the GameStop event. The TC can also be defined at the finer granularity of time to indicate the consistency of users’ concerns on the social network.

C. Comparison Analysis

In Section IV, we have known the importance of the influential users in the construction of the interaction networks. It inspires us to compare the influential users and common users in the topic aspect.

We chose the first two thousand users with the highest PageRank score as the influential users and others as the
common users. We first extracted the high-frequency words of the influential users and common users in each phase. The top-10 most common words in each phase are summarized in Table VI. Comparing their most common words, we find that their high-frequency words in their posts and comments are similar in all phases except the prehistory phase. In prehistory, the term "gme" appears in influential users’ high-frequency words but not in common users’, which indicates that the influential users followed the GameStop earlier than the common users.

Though the common words are similar, their concerned topics still exist differences. Fig. 11 shows the proportion of their dominant topic in each phase. The most significant difference between their topic distributions is that influential users discussed more topic 7 from the incubation phase to the fade phase. Two types of uses have similar topic distributions in other topics. We also find that influential users hardly concern the topics 9 and 10 during the GameStop short squeeze. That is, the influential users express few obscenities and other stocks except GME.

To better compare the topic characteristic between two types of users, we visualized their topic embedding in the 2-D space in Fig. 12. As shown in all subfigures in Fig. 12, the most influential users’ 2-D points appear close together in all phases, while the common users’ 2-D points scatter. Such phenomenon demonstrates that influential users’ topics are more centralized than common users’ topics.

VI. SENTIMENT ANALYSIS OF INTERACTION NETWORKS

Analyzing the user’s SP for investment is an essential aspect of understanding the influence of investors’ collective behaviors on the financial market. In this section, we examine the sentiment evolution of users on r/WSB during the GameStop short squeeze and measure the sentiment homophily and divergence in our interaction networks.

A. Sentiment Evolution Analysis

Investment sentiment on r/WSB is a user’s anticipation about the price development in a market. In this article, the...
Fig. 12. Two types of users’ topic embeddings in the 2-D space. The left subfigure represents the influential users’ scatter and the right is the common users’ scatter. (a) Prehistory. (b) Incubation. (c) Development. (d) Climax. (e) Fade.

VADER and SP dictionary which are introduced in Sections II and III are applied to identify the user’s SP. The polarity score is normalized to be between $-1$ (most extreme negative) and $+1$ (most extreme positive). Table VII gives the detailed statistical description of users’ SP score in each phase. Overall, the number of users with negative SP is higher than the number of users with positive SP for all phases. The average polarity score is close to zero, i.e., the whole sentiment is almost neutral. The large kurtosis means that many users’ polarity scores are close to zero. The positive skewness indicates that the tail of the polarity distribution is on the right.

We regard the users who have positive polarity scores as the positive users. Reversely, we regard the users who have negative polarity scores as the negative users. In that case, we can obtain the daily user number with different polarities.

Table VII

<table>
<thead>
<tr>
<th>Phase</th>
<th>#Negative</th>
<th>#Positive</th>
<th>Mean</th>
<th>Std</th>
<th>Kr.</th>
<th>Skew</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prehistory</td>
<td>34649</td>
<td>21739</td>
<td>-0.01</td>
<td>0.12</td>
<td>17.61</td>
<td>2.53</td>
</tr>
<tr>
<td>Incubation</td>
<td>26399</td>
<td>22568</td>
<td>0.02</td>
<td>0.17</td>
<td>9.20</td>
<td>2.42</td>
</tr>
<tr>
<td>Development</td>
<td>37226</td>
<td>37012</td>
<td>0.03</td>
<td>0.18</td>
<td>8.13</td>
<td>2.31</td>
</tr>
<tr>
<td>Climax</td>
<td>155642</td>
<td>144521</td>
<td>0.02</td>
<td>0.17</td>
<td>9.74</td>
<td>2.51</td>
</tr>
<tr>
<td>Fade</td>
<td>168028</td>
<td>149093</td>
<td>0.03</td>
<td>0.18</td>
<td>6.89</td>
<td>2.02</td>
</tr>
</tbody>
</table>

Fig. 13. Topic correlation of the influential users and common users. (a) Six types of topic correlations. (b) Correlation value on each day.

Fig. 14. Heat maps of the Pearson correlation coefficient of daily topics. The left subfigure is the common users’ similarity matrix, and the right subfigure is the influential users’ similarity matrix. Please note that the data on January 25 and 26 are missing. We used the linear insertion method to complete the values.
The daily number of users with different sentiment polarities is shown in Fig. 15. As our statistical result indicates that users with negative investment polarity are more than those with positive investment polarity on most days, we plotted the daily average polarity score curves of all users, negative users, and positive users in Fig. 16. The average polarity curve of all users slowly rises but is still below zero in the prehistory phase. After January 12, the cure of positive users has significantly increased, which leads to a positive average polarity score. However, the average score of negative users is steady in the prehistory phase and slowly decreases after January 12. Overall, although the proportion of users with positive polarity does not increase, their positive polarity strength has significantly improved during the GameStop short squeeze.

Moreover, we compared the sentiment polarities of influential users and common users in Fig. 17. In fact, their sentiment polarities do not have a significant difference before January 18, i.e., the end of the incubation phase. After that, common users show higher positive polarity scores than those of influential users, which demonstrates that common users have more positive investment leaning for GameStop's stock price in the development, climax, and fade phase. We also count the daily number of communities with negative polarity scores and positive polarity scores. The results are shown in Fig. 18. We can find that the number of negative communities is larger than the number of negative communities from January 16 to January 24.

Identifying the investment SP can help to extract meaningful sentimental topic words. We implemented LDA in the contents with positive scores to obtain the positive topic words. In the same way, the negative topic words are also extracted from the contents with negative scores. These words are listed in Table VIII, where 82 words only appear in the contents with positive scores, 67 words only appear in the contents with negative scores, and 55 words appear both in positive and negative contents. We can see some words and emoticons with strong positive investment tendency appear in the positive topic word list such as the mars 🌋, moon 🌒, and diamond ⭐. Similarly, some words and emoticons with strong negative investment tendency also appear in the negative topic word list such as lose, transfer, 🙄, and 😞. Some topic words have dual polarity despite their meanings such as buy, call, sell, and short.

### B. Evolution Analysis of Sentiment Homophily and Divergence

In the interaction networks, an interesting problem is whether a user will tend to interact with similar people who have similar SP during the GameStop short squeeze. In this section, we investigate the sentiment homophily and divergence in the interaction networks to reveal the potential user behavior under the short squeeze background.
A simple method to describe the sentiment homophily is comparing the focal user $i$’s $sp_i$ with his neighbor users set $N_i$’s $sp$. The neighbor users set $N_i$’s $sp$ is defined as the average polarity scores of individual users from $N_i$, i.e.,

$$\tilde{sp}_i = \frac{1}{|N_i|} \sum_{j \in N_i} s_j,$$

where $\tilde{sp}_i$ is the $sp$ of $N_i$ and $|N_i|$ is the number of users in $N_i$. We made a 2-D hexagonal binning plot of all points $(s_i, \tilde{sp}_i)$ in Fig. 19 and the value of the hexagon is determined by the number of points in the hexagon. As shown in Fig. 19, quadrant I has more points than quadrant IV in all phases, i.e., a user with a positive polarity score tends to interact with other users with positive polarity scores. Moreover, with the developing of the GameStop short squeeze, such a phenomenon is more obvious. On the contrary, there is no significant negative sentiment homophily because quadrant II and quadrant III have the roughly same size points in all phases. Considering a large number of users sticking around score zero, $x$-axis, $y$-axis, and origin have many points.

For the sentiment divergence (SD), we define the SD of a network at time $t$ as

$$sd(t) = \frac{1}{|N_i|} \sum_{j \in N_i} |s_i - \tilde{sp}_j|.$$

Then, we plotted the SD in Fig. 20. From Fig. 20, we observe that the SD grows wavy and the rising rate has an obvious improvement after January 7, which indicates that the SD between the adjacent users in the interaction

### TABLE VIII

<table>
<thead>
<tr>
<th>Sentimental Topic Words Extracted From Positive User’s Content and Negative User’s Content</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Positive topic words (82)</strong></td>
</tr>
<tr>
<td>1k, attack, await, better, bro, brother, come, crash, damn, delete, diamond, elon, end, enjoy, financial, forever, friday, gang, getting, gonna, good, got, great, happy, jack, jen, january, jesus, jmia, job, king, let’s, line, lol, long, loss, love, man, mars, melvin, moon, needs, next, nice, nok, oh, paper, plr, post, retard, rocket, ship, sold, stay, stop, strong, take, target, tendency, thank, thank, till, together, tels, two, wait, went, we’ve, won’t, work, yes, 🎁, 🎁, 🎁, 🎁, 🎁, 🎁, 🎁.</td>
</tr>
<tr>
<td><strong>Negative topic words (67)</strong></td>
</tr>
<tr>
<td>Account, actually, also, app, ass, bank, big, broker, business, cap, cash, citadel, chick, company, could, earning, ever, every, fidelity, fraud, future, gain, game, hour, investor, lose, manipulation, many, margin, media, minute, monday, morning, much, new, open, order, pay, position, put, real, retail, rh, rich, rule, see, shut, stimulus, sub, sure, system, tech, term, tesla, that, trade, transfer, use, value, volume, world, was, way, week, would, year.</td>
</tr>
</tbody>
</table>

**Notes**: We only contained the words whose weights are greater or equal to 0.01 for each topic.

### TABLE IX

**OLS Regression Results**

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coef.</th>
<th>S.E.</th>
<th>t-statistic</th>
<th>P &gt; [t]</th>
<th>0.025</th>
<th>0.01</th>
<th>0.005</th>
<th>0.001</th>
</tr>
</thead>
<tbody>
<tr>
<td>SMA</td>
<td>0.4558</td>
<td>0.022</td>
<td>21.028</td>
<td>0.000</td>
<td>0.413</td>
<td>0.498</td>
<td></td>
<td></td>
</tr>
<tr>
<td>DTP</td>
<td>0.1065</td>
<td>0.035</td>
<td>3.032</td>
<td>0.003</td>
<td>0.037</td>
<td>0.175</td>
<td></td>
<td></td>
</tr>
<tr>
<td>TC</td>
<td>0.4015</td>
<td>0.023</td>
<td>17.094</td>
<td>0.000</td>
<td>0.355</td>
<td>0.448</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SP</td>
<td>0.1950</td>
<td>0.021</td>
<td>9.235</td>
<td>0.000</td>
<td>0.153</td>
<td>0.237</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SD</td>
<td>-0.2848</td>
<td>0.021</td>
<td>-13.367</td>
<td>0.000</td>
<td>-0.327</td>
<td>-0.243</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**R-squared (uncentered)**: 0.870

**Adj. R-squared (uncentered)**: 0.869

**F-statistic**: 549.5

**Prob (F-statistic)**: 5.83E-179

**Log-Likelihood**: 303.83

**AIC**: -597.7

**BIC**: -577.5

**Notes**: $R^2$ is computed without centering (uncentered) since the model does not contain a constant. Standard Errors assume that the covariance matrix of the errors is correctly specified.

Except for the sentiment homophily, we further explore the sentiment divergence (SD). For the sentiment point $(s_i, \tilde{sp}_i)$, we define the SD of a network at time $t$ as $sd(t) = (1/|N_i|) \sum |s_i - \tilde{sp}_j|$. Then, we plotted the SD in Fig. 20. From Fig. 20, we observe that the SD grows wavy and the rising rate has an obvious improvement after January 7, which indicates that the SD between the adjacent users in the interaction

![Fig. 19. Hexagonal binning plot of all points $(s_i, \tilde{sp}_i)$ in each phase. The $x$-coordinate represents the focal user $i$’s sentiment score and the $y$-coordinate represents the average polarity score of $i$’s neighbors. (a) Prehistory. (b) Incubation. (c) Development. (d) Climax. (e) Fade.](image)

![Fig. 20. Daily SD. Please note that the data on January 25 and 26 are missing. We used the linear insertion method to complete the values.](image)
networks escalates with the development of the GameStop short squeeze.

VII. EXPLANATION OF GAMESTOP’S PRICE FROM INTERACTION NETWORKS

In Sections IV–VI, we investigated the characteristics of the collective behaviors and social dynamics in interaction networks constructed during the evolution of the GameStop event on r/WSB. These characteristics cover the evolutions of the topological structure, user’s topic, and sentiment. A clear fact is that some of the characteristics have considerable relationships with GameStop’s stock price. The important influence on social media for investment has been proven [34], [35], which inspires us whether these attributes can help us to explain the GameStop’s stock price.

According to the previous analysis, we construct five explanatory variables from three perspectives.

1) SMA measures the user’s activity level on r/WSB. From the perspective of the topological structure, we use the number of edges of the interaction network [see Fig. 3(b)] at time $t$ to indicate the SMA at time $t$.

2) Dominant topic popularity (DTP) measures the degree of concern about the topic which is discussed by most people at time $t$. DTP at time $t$ is defined as the proportion of the users who focus on dominant topic at time $t$. The definition of DTP is similar to the operation in Fig. 7.

3) TC measures the degree of topic dispersion, defined in Section V-B. Generally, the more dispersed the discussed topics are, the less information the topic distribution contains.

4) SP is the average value of the all users on r/WSB at time $t$, which depicts the sentiment trend of the whole social forum.

5) SD measures the degree of sentiment dispersion in the interaction network at time $t$, which has been defined in Section VI-B.

Finally, we exploit the linear regression to model the relationship between the stock price response $y$ and the five explanatory variables

$$y_t = \beta_1 \text{SMA}_{t-1} + \beta_2 \text{DTP}_{t-1} + \beta_3 \text{TC}_{t-1} + \beta_4 \text{SP}_{t-1} + \beta_5 \text{SD}_{t-1} + \epsilon_t \quad (1)$$

where $\beta_i$, $i = 1, \ldots, 5$ are the estimated regression parameters and $\epsilon_t$ is the error term. These parameters are estimated via ordinary least squares (OLS). The OLS regression results are reported in Table IX.

Considering the developing process, we collected a 15-min stock price from January 12 to February 3. The five explanatory variables are recalculated at the 15-min level. The response variable and explanatory variables are shown in Fig. 21. We report the estimated coefficients, standard errors, and corresponding model characteristics. $R^2$ and F-statistic show that our model adequately describes GameStop’s stock price in our sample period. The coefficients of SMA, DTP, TC, and SP are positive and significant. Therefore, the more the interaction of the users, the more popularity of the dominant topic, the higher cohesiveness of the discussed topics, and the more positive investment sentiment, the higher the next 15-min stock price is. Interestingly, the coefficient of SD is negative and significant, which indicates that the more SD among users on r/WSB, the lower the next 15-min stock price is. Our results suggest that part of GameStop’s stock price is driven by the SMA, popularity of the dominant topic, TC, SP of users, and SD between interacted users on r/WSB. We think it is a new and parsimonious way to analyze and predict the stock price from the unstructured social media data.

VIII. CONCLUSION

In January 2021, the users from subreddit r/WSB triggered an unprecedented short squeeze by driving up GameStop’s stock price to an unbelievable high point. The GameStop short squeeze highlights the significant role of social media in the propagation of investment ideas and the coordination of behaviors, as well as produces a research question about analyzing the collective behaviors and social dynamics characteristics of participants on the social media during the GameStop frenzy. The game of retail investors banding together to impact the financial market has just started. We must pay great attention to this emerging social phenomenon and deeply investigate its internally collective behavior and social dynamics mechanism.

In this article, we quantitatively investigate the characteristics of the dynamic interaction networks from the evolutions of the topological structure, discussed topics, and user’s SP by exploiting network construction technologies, topic modeling, and sentiment analysis.

1) For the topological structure, we found that the users’ collective behaviors tend to form the interaction networks on r/WSB, which have the topological structural superiority to transport and boost the diffusion of the investment information. And the interaction network evolves toward a small network while keeping robust scale-free property with the surge of the stock price.

2) For the evolution of the discussed topic, we observed that the topic distribution produces a significant change whether in individual level and community with the rise of the GameStop event and becomes more centralized, and the degree of topic dispersion of influential users is larger than that of common users.

3) For the evolution of the sentiment, we discovered that the collective SP slowly increases toward the positive
direction with the development of the GameStop short squeeze, but more users tend to hold negative polarity on most days, and the sentiment homophily and divergence become more and more significant.

4) Finally, we suggested that part of GameStop’s stock price is explained by the SMA, popularity of the dominant topic, TC, SP of users, and SD between interacted users on r/WSB by analyzing the relationships between price and social media.

Quantitatively characterizing the interaction networks and participants’ behaviors during the GameStop short squeeze contributes to the analysis of social system behavior and structure and provides valuable insights into financial practice and policy decision-making. These findings in this article may provide evidence to regulate financial behaviors. Based on these findings, we also provide a new and parsimonious way to analyze and predict the stock price from the unstructured social media data.

However, there are still many problems about the GameStop short squeeze to explore. We only consider the participants from r/WSB in this article, while other social media such as Twitter and mainstream news reports also influence the development of the hot event [36]. How to jointly model the influence from multiple social media platforms is a challenge [37] to social computing.

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[4] Melvin Capital Lost 53% in January, Hurt by GameStop and Other Bets—WSJ

Other Bets—WSJ


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Other Bets—WSJ


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